

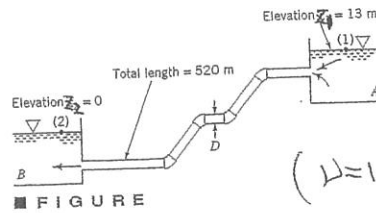
1001 機械系博士班資格考試題目

考試科目	方式	
流體力學	Closed Book, 可使用計算機	Part I

1. An atmosphere on a planet has a temperature of 15°C at sea level and drops 1°C per 500 m of elevation. The gas constant R for this atmosphere is 220 N·m/(kg·K). At what elevation is the pressure 30 percent that of sea level? Take $g = 9.00 \text{ m/s}^2$.

(10%) (Please derive the eq. first)

2. **GIVEN** Water at 15°C ($\nu = 1.12 \times 10^{-6} \text{ m}^2/\text{s}$) is to flow from reservoir A to reservoir B through a pipe of length 520 m and roughness $1.5 \times 10^{-4} \text{ m}$ at a rate of $Q = 1 \text{ m}^3/\text{s}$ as shown in Fig. The system contains a sharp-edged entrance and four flanged 45° elbows.



FIND Determine the pipe diameter needed. (Use Colebrook eq.)

$K_{ent} = 0.5, K_{elbow} = 0.2, K_{exit} = 1$

$(\nu = 1.12 \cdot 10^{-6} \text{ m}^2/\text{s})$

(15%)

Use Colebrook eq.

$$\frac{1}{\sqrt{f}} = -2.0 \log \left[\frac{\epsilon/D}{3.7} + \frac{2.51}{Re \sqrt{f}} \right]$$

3. The three components of velocity in a flow field are given by

$$\begin{aligned} u &= x^2 + y^2 + z^2 + xyz \\ v &= xy + yz + z^2 \\ w &= -3xz - z^2/2 + 4yz \end{aligned}$$

(15%)

(a) Determine the volumetric dilatation rate and interpret the results. (b) Determine an expression for the rotation vector. Is this an irrotational flow field?

4. Oil ($\mu = 0.4 \text{ N} \cdot \text{s}/\text{m}^2$) flows between two fixed horizontal infinite parallel plates with a spacing of 4 mm. The flow is laminar and steady with a pressure gradient of $-900 \text{ (N/m}^2\text{) per unit meter}$. Determine the volume flowrate per unit width and the shear stress on the upper plate.

(10%)

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1. Please describe the boundary layer structure and the thickness on a flat plate. Also define the displacement thickness. (15%)
2. Please derive the boundary layer equations and its boundary conditions. (start from 2-D Navier-Stokes equations) (20%)
3. For laminar flow in a round pipe of diameter D , at what distance from the centerline is the actual velocity equal to the average velocity? (15%)